# Stat 140: Inference for Simple Linear Regression Example - Wild Horses

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### Wild Horses

What is the relationship between the size of a herd of horses and the number of foals (baby horses!!) that are born to that herd in a year?

```
horses <- read_csv("https://mhc-stat140-2017.github.io/data/sdm4/Wild_Horses.csv")
```

```
## Parsed with column specification:
## cols(
## Foals = col_integer(),
## Adults = col_integer()
## )
head(horses)
```

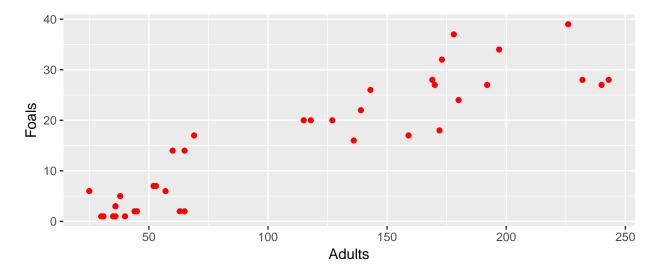
## # A tibble: 6 x 2 ## Foals Adults ## <int> <int> ## 1 28 232 ## 2 18 172 16 ## 3 136 ## 4 20 127 ## 5 20 118 ## 6 20 115 nrow(horses)

## [1] 38

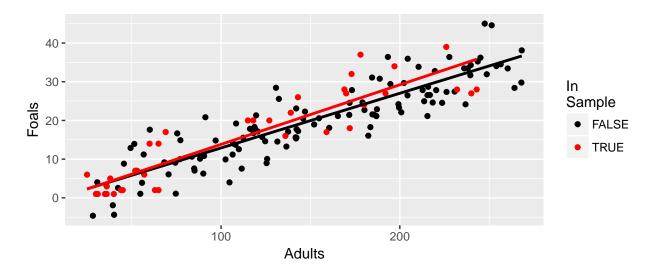
#### Questions to Start With:

- What is the observational unit?
- What are the variable data types (categorical or quantitative)?
  - Foals:
  - Adults:
- Which of these variables is the **explanatory** variable and which is the **response**?
  - Explanatory:
  - Response:

Previously: Fit linear regression to describe the relationship between number of adults and number of foals in the *sample*.



Today: Use data from this sample to learn about the relationship between number of adults and number of foals in the *population* 



#### (a) Are the assumptions for *inference* for the linear regression model met?

We'll add a new condition to our list for linear regression:

- Independence
  - Randomization/no connection between different observational units

To remember this, think of a helpful leprechaun named Patrick O'LINE:

- (No) Outliers
- Linear Relationship
- Independent Observations
- Normal Distribution of Residuals
- Equal Variance of Residuals

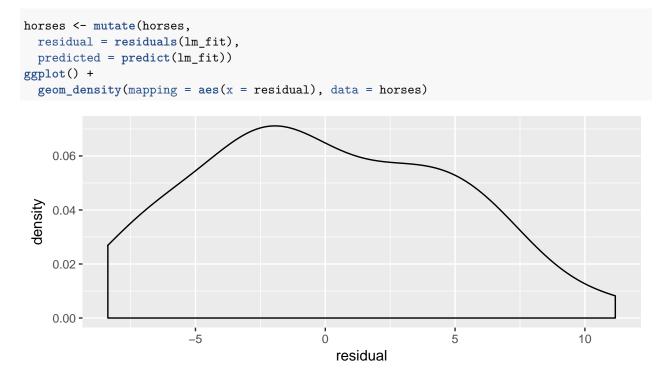


- (No) Outliers
- Linear Relationahip (Straight Enough)
- Independent Observations (Randomization)
- Normal Distribution of Residuals (Can't check this yet need to look at a histogram or density plot of the residuals after fitting the model)
- Equal Variance of Residuals (Does the Plot Thicken?)

```
(b) Fit the linear model
```

```
# format is: lm(response_variable ~ explanatory_variable, data = data_frame)
lm_fit <- lm(Foals ~ Adults, data = horses)</pre>
summary(lm_fit)
##
## Call:
## lm(formula = Foals ~ Adults, data = horses)
##
## Residuals:
##
              1Q Median
                            3Q
      Min
                                  Max
## -8.374 -3.312 -0.965 3.686 11.172
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -1.5784
                            1.4916
                                     -1.06
                                                0.3
                            0.0114
                                     13.49 1.2e-15 ***
## Adults
                 0.1540
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4.94 on 36 degrees of freedom
## Multiple R-squared: 0.835, Adjusted R-squared: 0.83
## F-statistic: 182 on 1 and 36 DF, p-value: 1.19e-15
```

(c) Check that the residuals follow a nearly normal distribution



(d) Explain in context what the regression says about the relationship between the number of adult horses in a herd and the number of foals born to that herd. Interpret both the intercept and the slope in context.

(e) Conduct a hypothesis test of the claim that when there are 0 adults in a herd, there will be 0 foals born to that herd.

(f) Draw a picture of a relevant t distribution for the hypothesis test in part (e) and shade in the region corresponding to the p-value. How would you calculate the p-value for part (e) using the pt function in R and the given estimate and standard error?

(g) Conduct a hypothesis test of the claim that there is no relationship between the number of adults in a herd and the number of foals who are born to that herd.

(h) Obtain a 99% confidence interval for the population intercept,  $\beta_0$ , and for the population slope,  $\beta_1$ . Interpret the confidence interval for  $\beta_1$  in context.

## Note that unlike every other confidence interval function we've looked at, ## we set the confidence level with an argument called level, not conf.level confint(lm\_fit, level = 0.99) ## 0.5 % 99.5 %

## 0.3% 99.3%
## (Intercept) -5.6347 2.478
## Adults 0.1229 0.185

(i) How would you calculate the confidence interval for part (f) using the qt function in R and the given estimate and standard error?

(j) Interpret the standard error for the slope using the "95" part of the 68-95-99.7 rule.